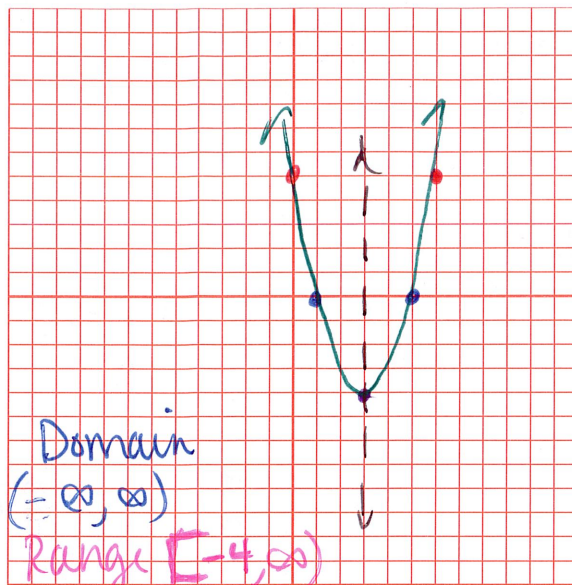


1) $f(x) = (x-3)^2 - 4$ opens up



Axis of Symm
 $x=3$

Domain $(-\infty, \infty)$
Range $[-4, \infty)$

① Vertex $(3, -4)$

② x-intercept Set $y=0$ Solve for x

$$0 = (x-3)^2 - 4$$

$$\sqrt{+4} = \sqrt{(x-3)^2}$$

$$\pm 2 = x-3$$

$$x = 3+2 \quad x = 3-2$$

$$x = 5 \quad x = 1$$

$(5, 0)$ $(1, 0)$

③ y-intercept Set $x=0$ solve for y

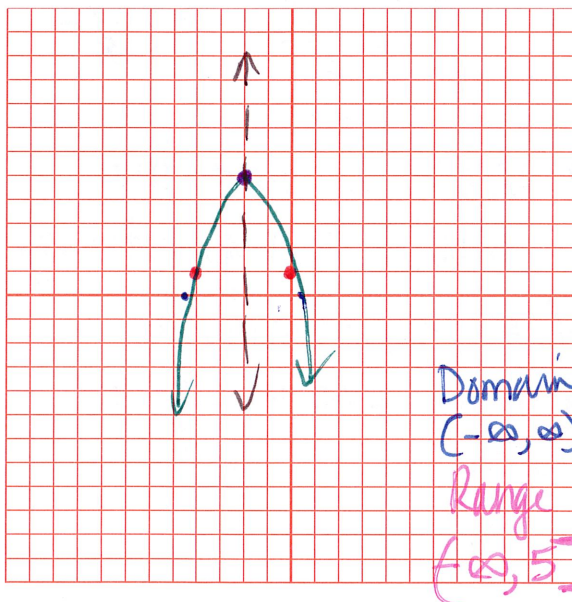
$$y = (0-3)^2 - 4$$

$$y = 9-4$$

$$y = 5$$

$(0, 5)$

2) $f(x) = 5 - (x+2)^2$



$x = -2$
Axis of Symm

Domain $(-\infty, \infty)$
Range $(-\infty, 5]$

Rewrite it as $f(x) = -(x+2)^2 + 5$

Vertex $(-2, 5)$ opens down

x-intercepts

$$0 = -1(x+2)^2 + 5$$

$$-5 = -1(x+2)^2$$

$$\sqrt{-5} = \sqrt{-1(x+2)^2}$$

$$\sqrt{5} = \sqrt{(x+2)^2}$$

$$x = -2 \pm \sqrt{5}$$

$(2.24, 0)$ $(-4.24, 0)$

y-intercept

$$y = -(0+2)^2 + 5$$

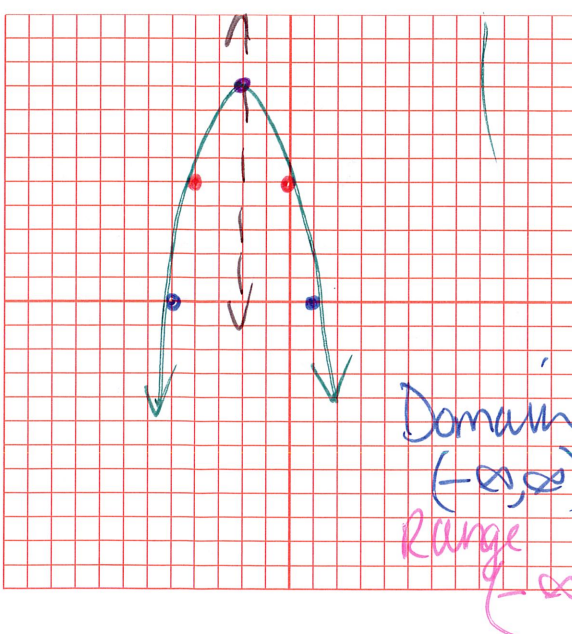
$$y = -4+5$$

$$y = 1$$

$(0, 1)$

3) $f(x) = -x^2 - 4x + 5$ opens down

Standard form so find Vertex $(-2, 9)$



Axis of Symm
 $x = -2$

Domain $(-\infty, \infty)$
Range $(-\infty, 9]$

$(\frac{-b}{2a}, P/c)$

$$-\frac{-4}{2(-1)} = \frac{4}{-2} = -2$$

$$y = 4 + 8 + 5$$

$$y = 4 + 5$$

x-intercept $0 = -1(x^2 + 4x - 5)$ factor

$$0 = -1(x+5)(x-1)$$

$$x = -5 \quad x = 1$$

y-intercept $(0, 5)$

#4 $f(x) = 3x^2 - 6x + 1$ opens up

Vertex $\left(\frac{-b}{2a}, p\right)$ $\frac{6}{2(3)}$

$(1, -2)$
Vertex

$3(1)^2 - 6(1) + 1$
 $3 - 6 + 1$
 $-3 + 1$

X-intercepts

$0 = 3x^2 - 6x + 1$
quad form

$X = \frac{+6 \pm \sqrt{(-6)^2 - 4(3)(1)}}{2(3)}$

$X = \frac{6 \pm \sqrt{36 - 12}}{2}$

$X = \frac{6 \pm \sqrt{24}}{2}$ $X = \frac{6 \pm \sqrt{4 \cdot 6}}{2}$

$X = 1 \pm \frac{\sqrt{6}}{3}$ $X = \frac{6 \pm 2\sqrt{6}}{2}$

$X = \frac{3 \pm \sqrt{6}}{3}$ $X = 1.82$
 $X = .18$

#5

$f(x) = (x-2)^2 (x+1)^3$

$X=2$ Mult 2 Love tap

$X=-1$ Mult 3 right through

degree of 5 John Travolta

Y-intercept set $x=0$ solve for y

$y = (0-2)^2 (0+1)^3$ $(0, 4)$
 $y = (4)(1)$

#6

$f(x) = -(x-2)^2 (x+1)^2$

Degree 4 negative leading Coeff
open down field goal

$X=2$ Mult 2 love tap

$X=-1$ Mult 2 love tap

Y-intercept $y = -(0-2)^2 (0+1)^2$

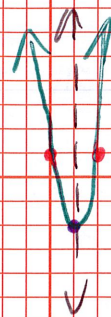
$y = -1(4)(1)$

$y = -4$ $(0, -4)$

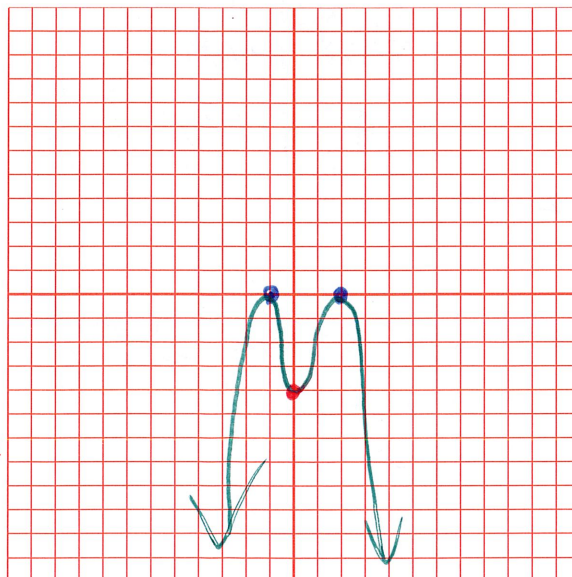
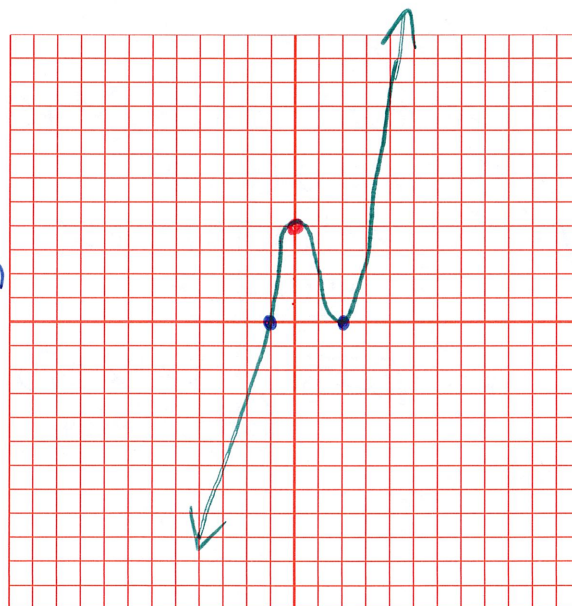
p.

axis of Sym

$X=1$



Domain $(-\infty, \infty)$
Range $[-2, \infty)$



#7 $f(x) = x^3 - x^2 - 4x + 4$

$\frac{p}{q}$ Possible rational roots graph on Calc

$\pm 1 \pm 2 \pm 4$

$\frac{\pm 1 \pm 2 \pm 4}{\pm 1}$

Roots look like $x = -2$ $x = 1$ $x = 2$

Check on Calc

John Travolta

With right hand goes right through

$\rightarrow (-2, 0)$
 $\rightarrow (1, 0)$
 $\rightarrow (2, 0)$

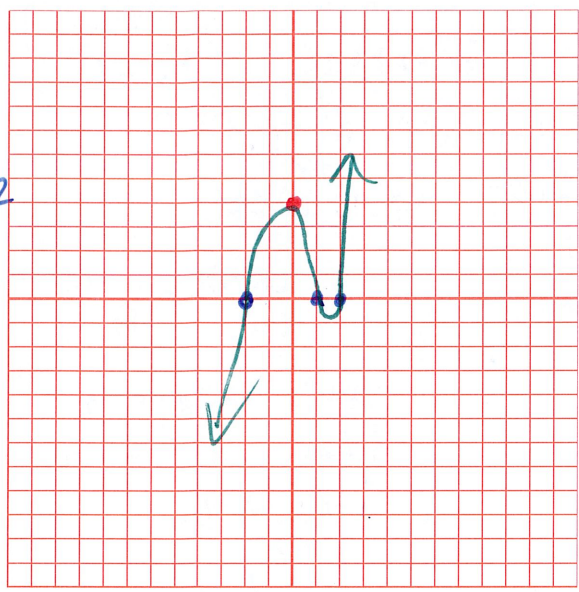
y-intercept $(0, 4)$

Could have boxed & circle factored

$x^3 - x^2 - 4x + 4$

$x^2(x-1) - 4(x-1)$

$(x^2 - 4)(x-1) = 0$ $(x+2)(x-2)(x-1) = 0$



#8 $f(x) = x^4 - 5x^2 + 4$

Call $x^2 = m$ Chunking

degree of 4
field goal

$(x^2)^2 - 5(x^2) + 4$

$m^2 - 5m + 4 = 0$

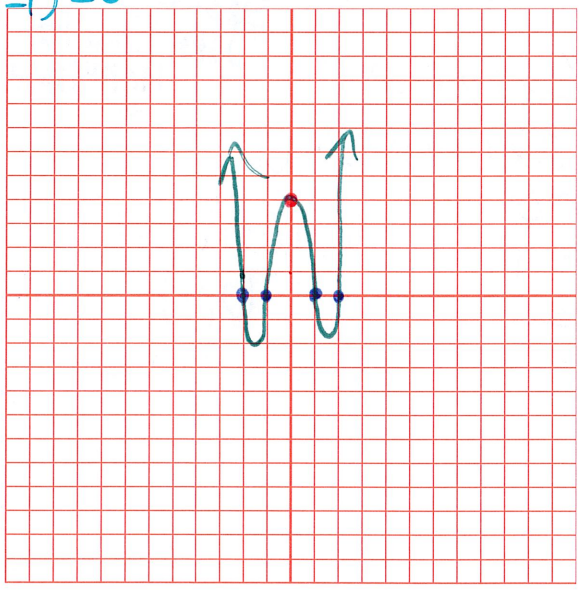
$(m-1)(m-4) = 0$

$m=1$
 $\sqrt{x^2} = \sqrt{1}$
 $x = \pm 1$

$m=4$
 $\sqrt{x^2} = \sqrt{4}$
 $x = \pm 2$

$(1, 0)$
 $(-1, 0)$
 $(2, 0)$
 $(-2, 0)$

y-intercept $(0, 4)$



#9 $f(x) = -(x+1)^6$

degree of 6 field goal opening down

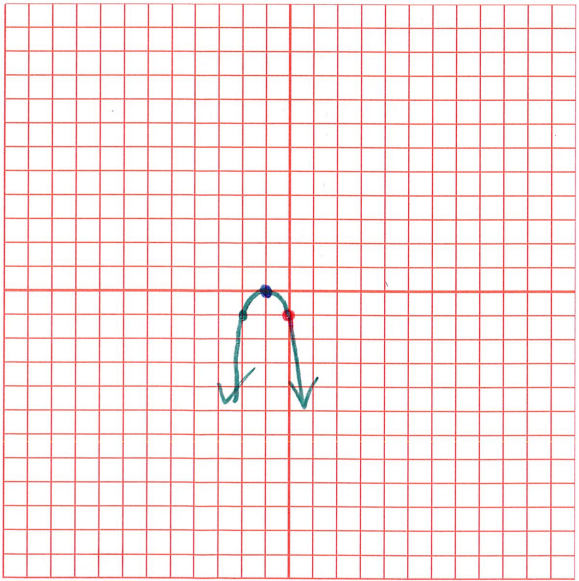
$x = -1$ Mult 6 love tap even mult

y-intercept set $x=0$

$y = -1(0+1)^6$ $(0, -1)$

$y = -1(1)$

$y = -1$



#10 $f(x) = -6x^3 + 7x^2 - 1$

John Travolta w/ left hand

$\frac{p}{q}$ Pool

$\frac{\pm 1}{\pm 1 \pm 2 \pm 3 \pm 6}$

$\frac{\pm 1 \pm \frac{1}{2}}{\pm \frac{1}{3} \pm \frac{1}{6}}$

Put in Calc to find

$x=1$ Root $(x-1)$ factor

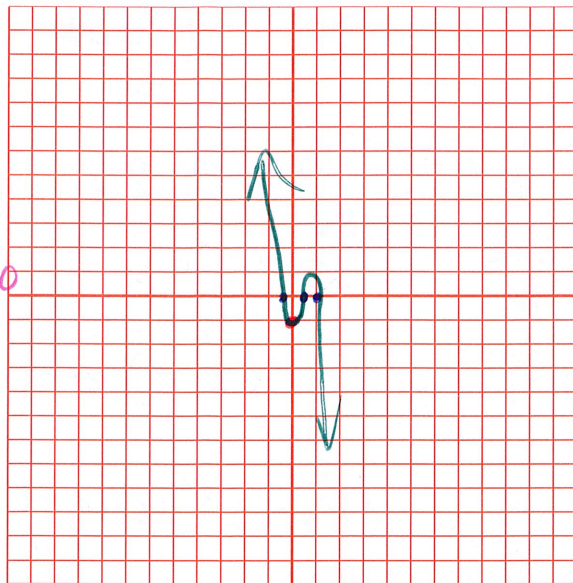
$$\begin{array}{r|rrrr} -6 & 7 & 0 & -1 \\ & \downarrow & -6 & 1 & 1 \\ \hline & -6 & 1 & 1 & 0 \end{array}$$

$(x-1)(-6x^2 + 13x + 1) = 0$
 $x=1$ factor

$x = -\frac{1}{3}$
 $x = \frac{1}{2}$
 $x = 1$

$-6x^2 + 13x + 1 = 0$
 $-3x(2x-1) - 1(2x-1) = 0$
 $(-3x-1)(2x-1) = 0$

y-intercept $(0, -1)$



#11 $f(x) = 2x^3 - 2x$ Cubic

factor

John Travolta right hand

$0 = 2x(x^2 - 1)$

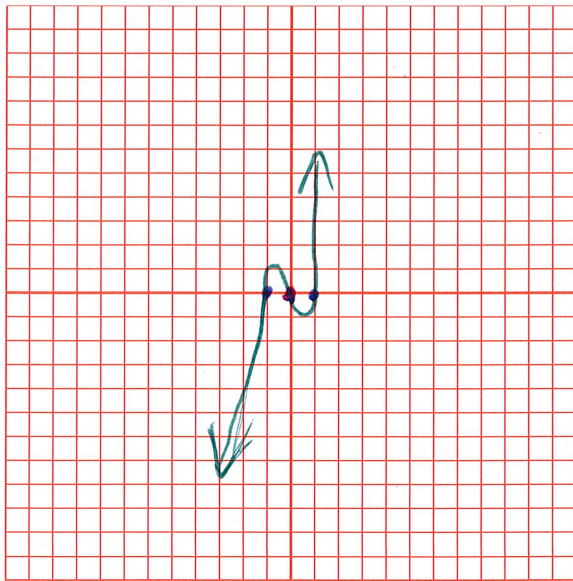
$0 = 2x(x+1)(x-1)$

$x=0$

$x=1$

$x=-1$

y-intercept $(0, 0)$



#12

$f(x) = x^3 - 2x^2 + 26x$

John Travolta right hand factor

$0 = x(x^2 - 2x + 26)$

$x=0$

Complete the Square

$x^2 - 2x + \square = -26 + \square$

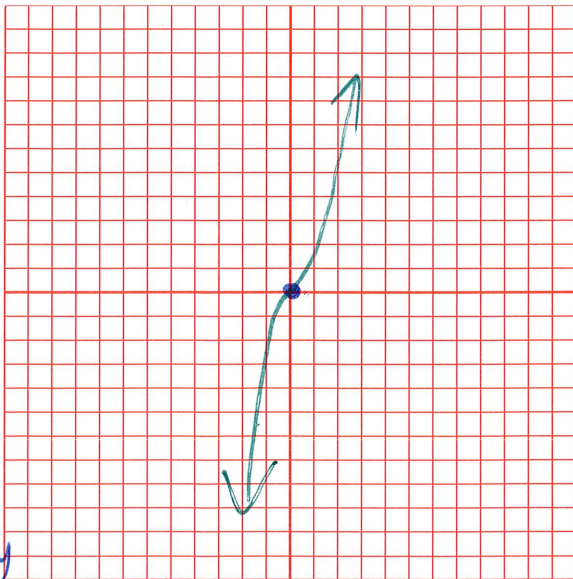
$\sqrt{(x-1)^2} = \sqrt{-25}$

$x-1 = \pm 5i$

$x = 1 \pm 5i$ 2 imaginary roots

$x=0$ 1 R root

$\begin{array}{r} x-1 \\ \hline x^2 - 2x + 1 \end{array}$



#13 $f(x) = -x^3 + 5x^2 - 5x - 3$ John Travolta w/ left hand pg. 5,6

Pool $\frac{p}{q} \frac{\pm 1 \pm 3}{\pm 1}$ $\begin{matrix} \pm 1 \\ \pm 3 \end{matrix}$
 Graph on Calc
 $x=3$ root $(x-3)$ factor

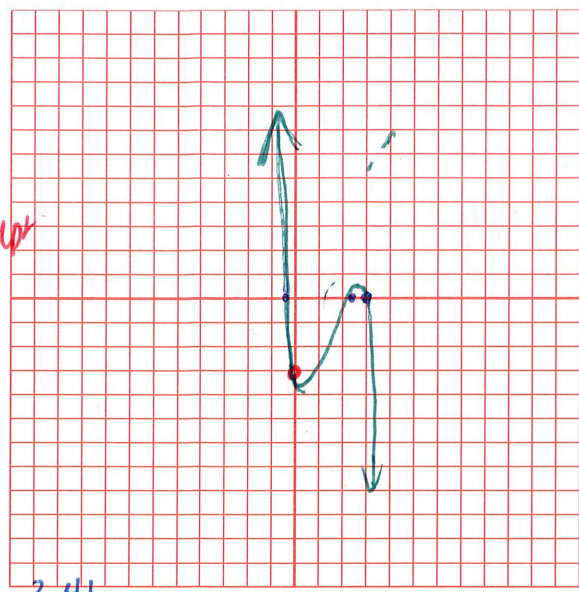
$$\begin{array}{r|rrrr} 3 & -1 & 5 & -5 & -3 \\ & \downarrow & -3 & 6 & 3 \\ \hline & -1 & 2 & 1 & 0 \end{array}$$

y-intercept
 $(0, -3)$

$(x-3)(-x^2+2x+1) = 0$
 $-1(x^2-2x-1)$ (complete the square)

x^2

$x^2 - 2x + \square = 1 + \square$ $x=3$
 $\sqrt{(x-1)^2} = \sqrt{2}$ $x=1+\sqrt{2}$ 2.41
 $x=1-\sqrt{2}$ -0.41
 $x=1 \pm \sqrt{2}$



Solve Each

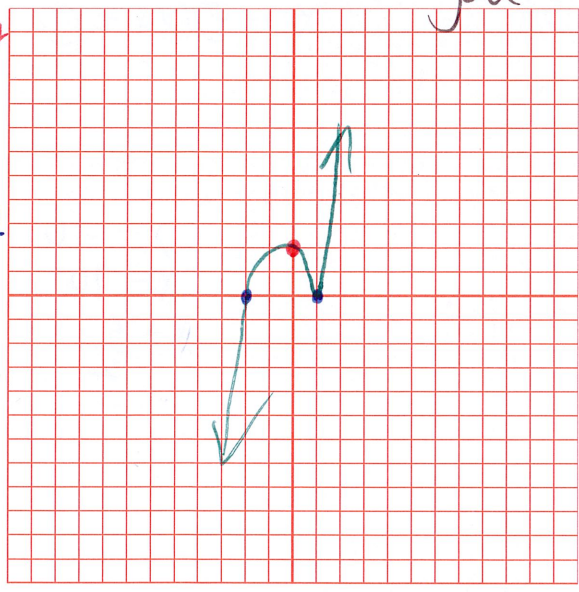
#14 $x^3 - 3x + 2 = 0$ y-intercept $(0, 2)$

$\frac{p}{q} \frac{\pm 1 \pm 2}{\pm 1}$ $\begin{matrix} \pm 1 \\ \pm 2 \end{matrix}$ $x = -2$
 $x = 1$ Mult 2
 low top

$(x+2)(x^2-2x+1) = 0$
 $(x+2)(x-1)(x-1) = 0$
 $x = -2$ $x = 1$ Mult 2

$$\begin{array}{r|rrrr} -2 & 1 & 0 & -3 & 2 \\ & \downarrow & -2 & 4 & -2 \\ \hline & 1 & -2 & 1 & 0 \end{array}$$

You don't have to graph I just did so you could see



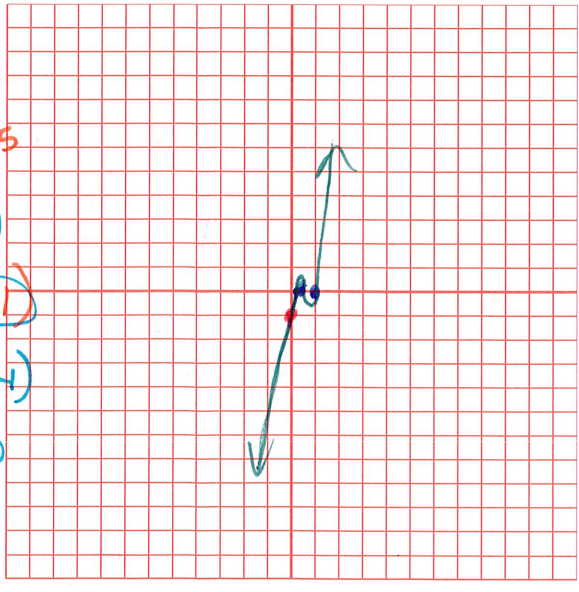
#15 $6x^3 - 11x^2 + 6x - 1 = 0$

$\frac{p}{q} \frac{\pm 1}{\pm 1 \pm 2 \pm 3 \pm 6}$ $\begin{matrix} \pm 1 \\ \pm \frac{1}{2} \pm \frac{1}{3} \\ \pm \frac{1}{6} \end{matrix}$
 $x=1$ root

factor $\frac{6}{-2, -3, -5}$

$(x-1)(6x^2-5x+1)$
 $(x-1)(6x^2-3x-2x+1)$
 $(x-1)(3x(2x-1)-1(2x-1))$
 $(x-1)(3x-1)(2x-1) = 0$
 $x=1$ $x=\frac{1}{3}$ $x=\frac{1}{2}$
 y-inter $(0, -1)$

$$\begin{array}{r|rrrr} 1 & 6 & -11 & 6 & -1 \\ & \downarrow & 6 & -5 & 1 \\ \hline & 6 & -5 & 1 & 0 \end{array}$$



#16

Should have 5 roots

John Travolta

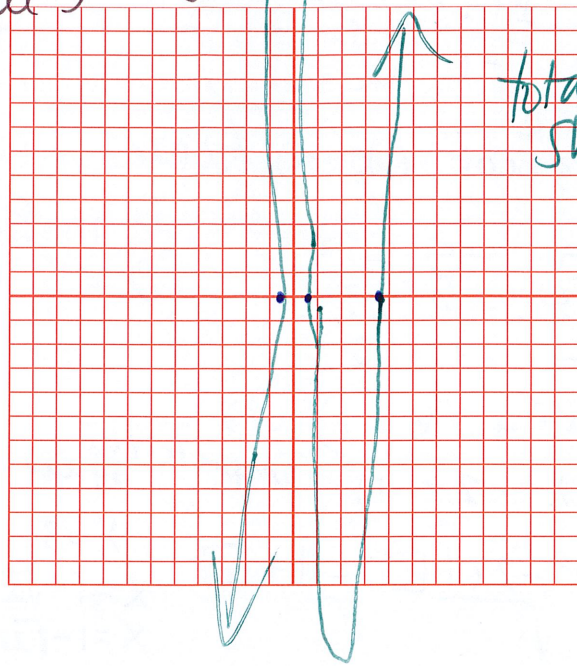
$$(2x+1)(3x-2)^3(2x-7) = 0 \text{ degree } 5$$

$$x = -\frac{1}{2} \quad x = \frac{2}{3} \text{ Mult } 3$$

$$x = \frac{7}{2} = 3\frac{1}{2}$$

y-intercept

$$(2(0)+1)(3(0)-2)^3(2(0)-7) \\ (1)(-8)(-7) \\ \text{So } (0, 56)$$



#17

$$2x^3 + 5x^2 - 200x - 500 = 0$$

Box & Circle factor

$$x^2(2x+5) - 100(2x+5) = 0$$

$$(x^2 - 100)(2x+5) = 0$$

$$(x+10)(x-10)(2x+5) = 0$$

$$x = -10 \\ x = 10 \\ x = -\frac{5}{2}$$

I am not graphing this one

$$\#18 \quad x^4 - x^3 - 11x^2 = x + 12$$

Set = to 0

$$x^4 - x^3 - 11x^2 - x - 12 = 0$$

$$\frac{p}{q} \quad \begin{matrix} \pm 1 \pm 2 \pm 6 \\ \pm 3 \pm 4 \pm 12 \end{matrix}$$

$$\frac{\pm 1 \pm 2 \pm 3 \pm 4 \pm 6 \pm 12}{\pm 1}$$

x = -3 on calc is a root

$$\text{factor } (x+3)$$

$$\begin{array}{r|rrrrr} -3 & 1 & -1 & -11 & -1 & -12 \\ & \downarrow & -3 & 12 & -3 & 12 \\ \hline & 1 & -4 & 1 & -4 & 0 \end{array}$$

$$(x+3)(x^3 - 4x^2 + 1x - 4)$$

$$\frac{p}{q} \quad \begin{matrix} \pm 1 \pm 2 \pm 4 \\ \pm 1 \end{matrix}$$

$$x = 4 \text{ root } (x-4)$$

factors

$$(x+3)(x-4)(x^2+1) = 0$$

$$x = -3 \quad x = 4 \\ x = i \quad x = -i$$

↑ solve for x

$$x^2 + 1 = 0 \quad \sqrt{x^2} = \sqrt{-1} \quad x = \pm i$$

4 roots
degree of 4
2 Real Root
x = -3
x = 4
2 Imag
x = i
x = -i

#19 $2x^4 + x^3 - 17x^2 - 4x + 6 = 0$

$\frac{p}{q}$

$\frac{\pm 1 \pm 2 \pm 3 \pm 6}{\pm 1 \pm 2}$

on Calc $X = -3$
root

$(X+3)$ factor

$$\begin{array}{r|rrrrr} -3 & 2 & 1 & -17 & -4 & 6 \\ & \downarrow & -6 & 15 & 6 & -6 \\ \hline & 2 & -5 & -2 & 2 & 0 \end{array}$$

$(X+3)(2x^3 - 5x^2 - 2x + 2)$

no do it again

$\frac{p}{q} \frac{\pm 1 \pm 2}{\pm 1 \pm 2}$

$\frac{\pm 1 \pm 1}{\pm 2 \pm 2}$

on Calc

$X = \frac{1}{2}$

factor

$(X - \frac{1}{2})$

$$\begin{array}{r|rrrr} \frac{1}{2} & 2 & -5 & -2 & 2 \\ & \downarrow & 1 & -2 & 2 \\ \hline & 2 & -4 & -4 & 0 \end{array}$$

$(X+3)(X - \frac{1}{2})(2x^2 - 4x - 4) = 0$

$X = 3$
 $X = \frac{1}{2}$
 $X = 1 - \sqrt{3}$
 $X = 1 + \sqrt{3}$

now factor

$2(x^2 - 2x - 2) = 0$

complete the square

$\begin{array}{|c|} \hline x^2 \\ \hline -x \\ \hline \end{array}$

$x^2 - 2x + 1 = 2 + 1$

$(x-1)^2 = 3$

$x-1 = \pm\sqrt{3}$

$x = 1 \pm \sqrt{3}$

all 4 roots

#20 $p(x) = -x^2 + 150x - 4425$

$x = \#$ Cabinets Sold per day

$p(x) =$ daily profit $\rightarrow x$

a) How many Cabinets should they sell to MAXIMIZE their profits $p(x)$

all you need to do is find your vertex

$(\frac{-b}{2a}, p(c))$

$\frac{-150}{2(-1)}$

$(75, \$1200)$

$-1(75)^2 + 150(75) = 4425$

$-5625 + 11250 - 4425$

6750

If you sell 75 Cabinets per day you will maximize your profit of \$1200.

next
next

#21 Pairs of #'s whose sum is -18
Maximize the product

X is first # then second # is

$$X(-18-X) = f(x)$$

$$X + (\text{second}) = -18$$

$$\text{Second \#} = -18 - X$$

$$-18x + x^2 = f(x)$$

$$-x^2 - 18x = f(x)$$

$$-(-9)^2 - 18(-9) =$$

$$-81 + 162$$

$$81$$

find vertex (Maximum) $\left(\frac{-b}{2a}, p/c\right)$

$$\frac{18}{2(-1)} \quad (-9, 81)$$

First # is going to be -9
Second # $-18 - (-9)$

Watch

$$(-9) + (-9) = -18$$

Sum is -18

Product is the Max

$$(-9)(-9) = 81$$

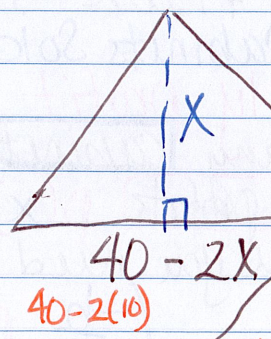
$$-18 + 9$$

Second # is $\rightarrow -9$

Two numbers are
 -9 & -9 .

#22

X = height of triangle
base = $40 - 2X$
 $A = \frac{1}{2} b \cdot h$



Maximize the

$$A(x) = \frac{1}{2}(40-2x)x$$

$$A(x) = \frac{1}{2}x(40-2x)$$

$$A(x) = 20x - 1x^2$$

$$A(x) = -x^2 + 20x$$

Now find vertex

height $\rightarrow \left(\frac{-b}{2a}, p/c\right)$
max area

$$\frac{-20}{2(-1)}$$

So if the height of the triangle is 10 inches the base would be 20 which would give you a max area of 100 square inches

$$-1(10)^2 + 20(10)$$

$$-100 + 200$$

$$100$$

you must long divide only this one

#23 $6x^4 - 3x^3 - 11x^2 + 2x + 4$

$$\begin{array}{r}
 3x^2 - 1 \\
 2x^2 - x + 3 \\
 \hline
 3x^2 + 0x - 1 \overline{) 6x^4 - 3x^3 - 11x^2 + 2x + 4} \\
 - 6x^4 + 0x^3 - 2x^2 \\
 \hline
 -3x^3 + 9x^2 + 2x \\
 - -3x^3 + 0x^2 + x \\
 \hline
 9x^2 + 1x + 4 \\
 - 9x^2 + 0x - 3 \\
 \hline
 1x + 1 \text{ Remainder}
 \end{array}$$

$x^2(3x^2 + 0x + 1)$

$-x(3x^2 + 0x - 1)$
 $3(3x^2 + 0x - 1)$

Answer $2x^2 - x + 3 + \frac{x+1}{3x^2-1}$

#24 you can synthetic divide

$2x^4 - 13x^3 + 17x^2 + 18x - 24$
 $x - 4$

4	2	-13	17	18	-24
	↓	8	-20	-12	24
	2	-5	-3	6	0

Answer $2x^3 - 5x^2 - 3x + 6$

#25 $n=3$ means degree is 3 you know the roots
 $x=1$ and $x=i$ $x=-i$

So the factors are
 $(x-1)(x-i)(x+i)$
 $(x-1)(x-i)(x+i)$
 $x^2 + xi - xi - i^2$

this will not be on quiz

$(x-1)(x^2+1)$

$x^3 + x - x^2 - 1$

you know $f(-1) = 8$
 $(-1, 8)$

$x^3 - x^2 + x - 1$

Answer
 $f(x) = -2(x^3 - x^2 + x - 1)$
 $f(x) = -2x^3 + 2x^2 - 2x + 2$

$8 = (-1)^3 - (-1)^2 + (-1) - 1$ $a_n = -2$

$8 = -1 - 1 - 1 - 1 (a_n)$
 $8 = -4(a_n)$

not on
quiz

#26 $n=4$ degree is 4 so 4 roots

$x=2$ Mult 2 $3i$ is a root so is $-3i$

$$(x-2)(x-2)(x-2)^2(x-3i)(x-(-3i))$$

$$(x-2)(x-2)(x-3i)(x+3i)$$

$$(x^2-4x+4)(x^2+9)$$

$$x^2+3xi-3xi-9i^2$$

$$x^4 + 9x^2 - 4x^3 - 36x + 4x^2 + 36$$

$$f(0) = 36$$

$$f(x) = x^4 - 4x^3 + 13x^2 - 36x + 36$$

$a_n = 1$ answer

$$y = a_n (x-2)^2 (x^2+9)$$

$$36 = a_n (0-2)^2 (0^2+9)$$

$$36 = a_n (4)(9)$$

$$\frac{36}{36} = \frac{36 a_n}{36}$$

$$1 = a_n$$

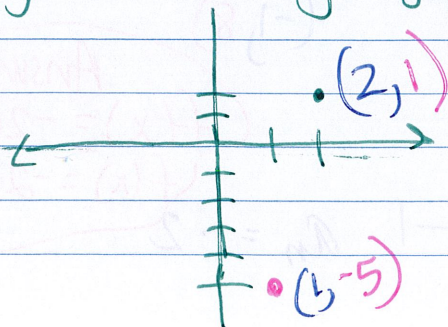
#27 Does $f(x) = x^3 - x - 5$ have a root between 1 & 2

use $f(1) = (1)^3 - (1) - 5 = 1 - 1 - 5 = -5$

$f(2) = (2)^3 - (2) - 5$

$$8 - 2 - 5 = 1$$

Yes there must be a root between 1 & 2 because when you plug in $x=1$ you get -5 and when you plug in $x=2$ you get 1 . So



It has to cross x-axis somewhere in between??