

Climb the Ladder 3.4 3.5

State the possible number of positive and negative zeros for each function.

degree  
5, 3, 1  
Real

1)  $f(x) = 3x^5 - 9x^4 + x^3 - 3x^2 - 24x + 72$

- (A) Possible # positive real zeros: 4, 2, or 0
- Possible # negative real zeros: 1
- (B) Possible # positive real zeros: 4, 2, or 0
- Possible # negative real zeros: 0
- (C) Possible # positive real zeros: 4, 2, or 0
- Possible # negative real zeros: 3
- (D) Possible # positive real zeros: 5, 3, or 1
- Possible # negative real zeros: 1

Goody's hand game and DeCartes Rule

4 positive  
Sign change  
4, 2, 0  
positive  
negative  
1 Sign change

2)  $f(x) = 2x^6 + x^4 - 50x^2 - 25$

- (A) Possible # positive real zeros: 0
- Possible # negative real zeros: 1
- (B) Possible # positive real zeros: 1
- Possible # negative real zeros: 2
- (C) Possible # positive real zeros: 1
- Possible # negative real zeros: 1
- (D) Possible # positive real zeros: 2 or 0
- Possible # negative real zeros: 0

Sign  
Sign changes  
Positive  
1 Sign change  
Negative  
+ + - -  
1 negative change

State the number of complex roots, the possible number of real and imaginary roots, and the possible rational roots for each equation. Use Goody's hand game. YOU DO NOT HAVE TO SOLVE

Pool Poss

3)  $x^3 - 5x^2 + 4x - 20 = 0$

3 R 0 Imag  
1 R 2 Imag

±1  
±2 ±4  
±5 ±10  
±20

4)  $x^5 + 3x^4 - 2x^3 - 6x^2 - 3x - 9 = 0$

5 R 0 Imag  
3 R 2 Imag  
1 R 4 Imag

±1 ±3 ±9  
±1

±1 ±3  
±9

State all the possible rational zeros for each function. Find the pool of possibilities then find all roots. YOU MUST FIND ALL ROOTS even if they are imaginary

5)  $x^3 - 2x^2 - 2x + 4 = 0$

±1 ±2 ±4

±2  
±1 ±4

6)  $x^3 - 3x^2 + x - 3 = 0$

±1 ±3

Use Calc to  
And root  
root is  $x=3$   
(x-3) factor

$x=2$   
(x-2) factor  
now synthetic divide to find other factor

2 | 1 -2 -2 4  
   ↓ 2 0 -4  
   ---  
   1 0 -2 0

(x-2)(x^2-2) = 0 Now solve  
 $x=2$   $x^2-2=0$   
 $x = \pm\sqrt{2}$

3 | 1 -3 1 -3  
   ↓ 3 0 3  
   ---  
   1 0 1 0

(x-3)(x^2+1) = 0 now solve  
 $x=3$   $x^2+1=0$   
 $x = \pm i$   $x^2 = -1$   
1 R 2 Imag

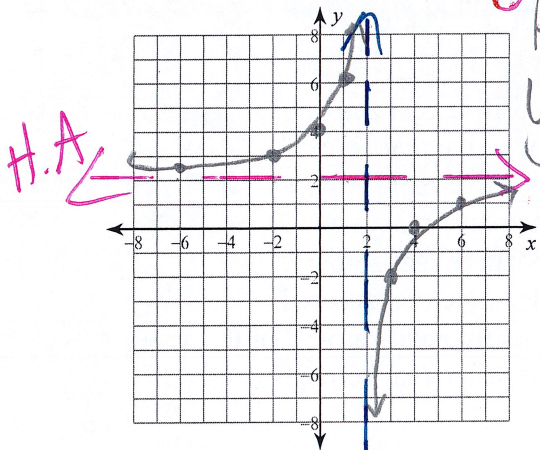
# h k Method

Graph each function. Draw all Asymptotes state any points of discontinuity

7)  $f(x) = -\frac{4}{x-2} + 2$

$x=2$  V.A  
 $y=2$  H.A

Parent  
 $y = -\frac{4}{x}$



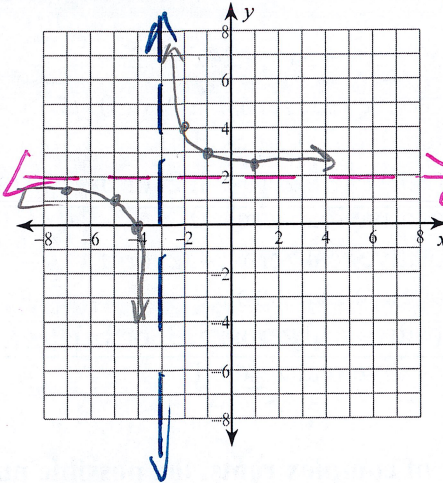
X	Y
-8	1/2
-4	1
-2	2
-1	4
1	-4
2	-2
4	-1
8	-1/2

$x \neq 2$

8)  $f(x) = \frac{2}{x+3} + 2$

$x=-3$  V.A  
 $y=2$  H.A

Parent  
 $y = \frac{2}{x}$



X	Y
-4	-1/2
-2	-1
-1	-2
1	2
2	1
4	1/2

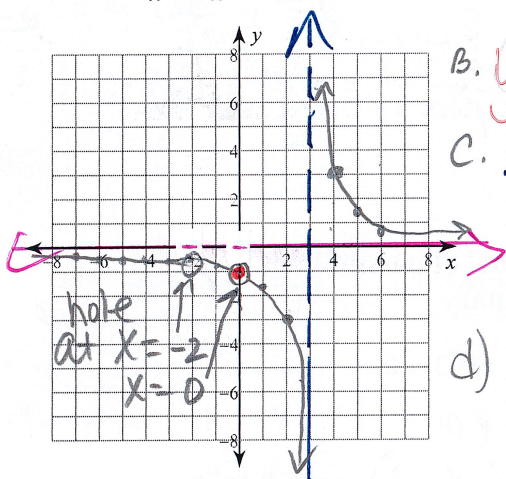
Use your seven steps to graph. State all the points of discontinuity and draw ALL asymptotes. SHOW ALL WORK

9)  $f(x) = \frac{+3x^2 + 6x}{x^3 - x^2 - 6x}$

change that to a positive

A. factor first

$$\frac{-3x(x+2)}{x(x^2-x-6)} = \frac{-3x(x+2)}{x(x+2)(x-3)}$$



B. y-intercept (0, -1)

Simplify First  $\frac{3}{x-3}$   $y = \frac{3}{0-3} y = -1$

C. X-intercept

Set numerator = 0 Simplify  $\rightarrow \frac{3}{x-3}$

0 = 3 None

d) find Vertical Asymptotes or holes

$$\frac{3x(x+2)}{x(x+2)(x-3)}$$

hole at  $x=0$

$x=-2$

$x=3$  V.A

$y = \frac{3}{x-3}$

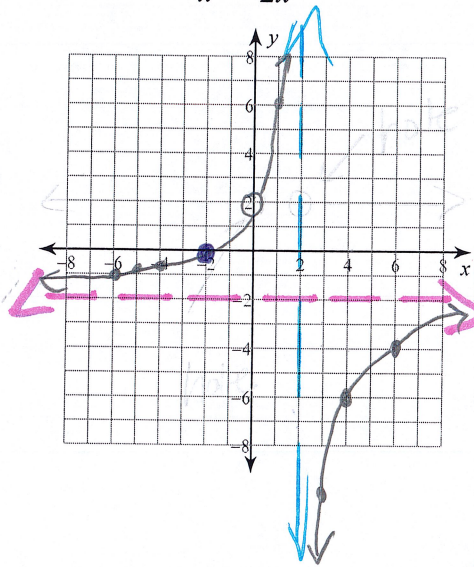
e) Horizontal Asymptotes  $n < m$   $y=0$

f) Use Calc to get points

-7	-.3
-6	-.333
-5	-.375
-4	-.429
-3	-.5
-2	error hole
-1	-.75
0	hole
1	-1.5
2	-3
3	V.A error
4	3

X	Y
5	1.5
6	1
7	.75
8	.6

10)  $f(x) = \frac{-2x^2 - 4x}{x^2 - 2x}$



factor first  $\frac{-2x(x+2)}{x(x-2)}$

$\frac{x}{x}$  divides out so  $x=0$  hole

Simplify hole at  $x=0$   $\frac{-2(x+2)}{(x-2)}$

y intercept Set  $x=0 = -2$

None because its a hole

$\frac{-2(0+2)}{(0-2)}$

(0,0) but hole so y-inter

x-intercept Set numerator = 0  $-2(x+2) = 0$

$(-2, 0)$

$x+2 = 0$   
 $x = -2$

V.A.  $x=2$  hole @  $x=0$

H.A.  $n=m$  so  $y = \frac{-2}{1} y = -2$

points from Calc

State the number of complex roots, the possible number of real and imaginary roots, and the possible rational roots for each equation. Then find all roots.

11)  $x^3 + 7x^2 + 12x + 10 = 0$  all steps 3 roots

$\frac{p}{q}$   $\pm 1 \pm 2$   
 $\pm 5 \pm 10$

now graph on calculator to find a root

$-5 = x$  root factor  
( $x+5$ ) now synthetic divide to find other factor

$$\begin{array}{r|rrrr} -5 & 1 & 7 & 12 & 10 \\ & & -5 & -10 & -10 \\ \hline & 1 & 2 & 2 & 0 \end{array}$$

( $x+5$ ) ( $x^2 + 2x + 2$ ) = 0  
 $x = -5$  Complete the square now solve  
 $x^2 + 2x + \square = -2 + \square$



$\sqrt{(x+1)^2} = \sqrt{-1}$

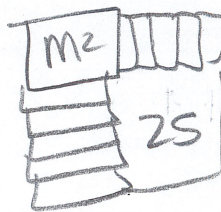
$x+1 = \pm i$   
 $x = -1 \pm i$  2 imag  
 $x = -5$  1 real 3-root

12)  $x^4 + 10x^2 + 21 = 0$  4 roots chunk

$(x^2)^2 + 10x^2 + 21 = 0$   $m = x^2$

$m^2 + 10m + 21 = 0$  Complete the square if you don't want to factor

$m^2 + 10m + \boxed{25} = -21 + \boxed{25}$



$\sqrt{(m+5)^2} = \sqrt{4}$

$m+5 = \pm 2$

$m+5 = 2$   $m+5 = -2$   
 $m = -3$   $m = -7$

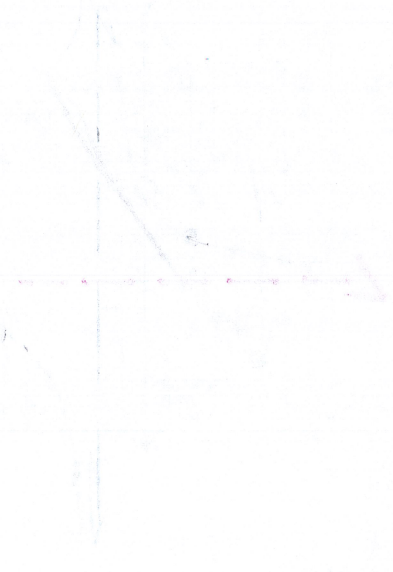
$\sqrt{x^2} = \sqrt{-3}$   $\sqrt{x^2} = \sqrt{-7}$   
 $x = \pm i\sqrt{3}$   $x = \pm i\sqrt{7}$

4 answers

Could factor also  
 $(m+7)(m+3)$   
 $m = -7$   $m = 3$

$$f(x) = \frac{1}{x^2} = x^{-2}$$

$$f'(x) = -2x^{-3} = -\frac{2}{x^3}$$



$f(x) = x^{-2}$   
 $f'(x) = -2x^{-3}$   
 $f''(x) = 6x^{-4} = \frac{6}{x^4}$

$x = m$   
 $u = x^2$   
 $(x^2) \cdot (x^2)$

$M$   $M$



$x = \text{true } (x^2 + m^2)$   
 $x^2 = 3 \quad x^2 = 1$